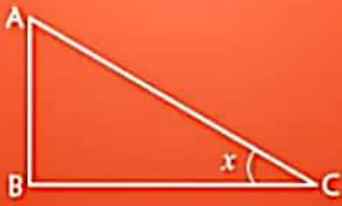


TRIGONOMETRIC IDENTITIES

Part I

1

Quotient Identities



$$\tan x = \frac{\sin x}{\cos x}$$

$$\cot x = \frac{\cos x}{\sin x}$$

$$\sec x = \frac{1}{\cos x}$$

$$\operatorname{cosec} x = \frac{1}{\sin x}$$

2

Pythagorean Identities



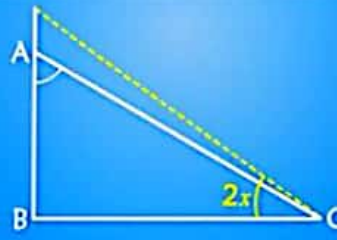
$$\sin^2 x + \cos^2 x = 1$$

$$\sec^2 x - \tan^2 x = 1$$

$$\operatorname{cosec}^2 x - \cot^2 x = 1$$

3

Double Angle Identities



$$\sin 2x = 2 \sin x \cos x$$

$$\cos 2x = \cos^2 x - \sin^2 x$$

$$\cos 2x = 2 \cos^2 x - 1$$

$$\cos 2x = 1 - 2 \sin^2 x$$

$$\cos 2x = \frac{1 - \tan^2 x}{1 + \tan^2 x}$$

$$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$$

4

Half Angle Identities



$$\sin \frac{x}{2} = \pm \sqrt{\frac{1 - \cos x}{2}}$$

$$\cos \frac{x}{2} = \pm \sqrt{\frac{1 + \cos x}{2}}$$

$$\tan \frac{x}{2} = \pm \sqrt{\frac{1 - \cos x}{1 + \cos x}}$$

$$\tan \frac{x}{2} = \frac{1 - \cos x}{\sin x}$$

$$\tan \frac{x}{2} = \frac{\sin x}{1 + \cos x}$$

TRIGONOMETRIC IDENTITIES

Part II

5

Angle Sum & Difference Identities



$$\sin (A \pm B) = \sin A \cos B \pm \cos A \sin B$$

$$\cos (A \pm B) = \cos A \cos B \mp \sin A \sin B$$

$$\tan (A \pm B) = \frac{\tan A \pm \tan B}{1 \mp \tan A \tan B}$$

$$\cot (A \pm B) = \frac{\cot A \cdot \cot B \mp 1}{\cot B \pm \cot A}$$

6

Sum Identities



$$\sin C + \sin D = 2 \sin \left(\frac{C+D}{2} \right) \cdot \cos \left(\frac{C-D}{2} \right)$$

$$\sin C - \sin D = 2 \cos \left(\frac{C+D}{2} \right) \cdot \sin \left(\frac{C-D}{2} \right)$$

$$\cos C + \cos D = 2 \cos \left(\frac{C+D}{2} \right) \cdot \cos \left(\frac{C-D}{2} \right)$$

$$\cos C - \cos D = -2 \sin \left(\frac{C+D}{2} \right) \cdot \sin \left(\frac{C-D}{2} \right)$$

7

Product Identities



$$2 \sin A \cos B = [\sin (A+B) + \sin (A-B)]$$

$$2 \cos A \sin B = [\sin (A+B) - \sin (A-B)]$$

$$2 \cos A \cos B = [\cos (A-B) + \cos (A+B)]$$

$$2 \sin A \sin B = [\cos (A-B) - \cos (A+B)]$$

8

Summation of Trigonometric Series



$$\begin{aligned} & \sin A + \sin (A+B) + \sin (A+2B) \\ & \quad + \dots + \sin (A+(n-1)B) \\ & = \frac{\sin nB/2}{\sin B/2} \cdot \sin \left(A + \frac{(n-1)B}{2} \right) \end{aligned}$$

$$\begin{aligned} & \cos A + \cos (A+B) + \cos (A+2B) \\ & \quad + \dots + \cos (A+(n-1)B) \\ & = \frac{\sin nB/2}{\sin B/2} \cdot \cos \left(A + \frac{(n-1)B}{2} \right) \end{aligned}$$